

# Microwave Integrated Circuits

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# Microwave Integrated Circuits

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# List of symbols

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## A) Physical quantities

$a$	waveguide width; parameter of the Richards' transformation; parameter of the coplanar line
$b$	waveguide height
$B$	parameter of the Richards' transformation
$B_a, B_b$	susceptance
$c$	light velocity in vacuum
$C, C_c$	capacitance, collector-base capacitance
$d$	distance of the lateral wall from the line
$e$	distance of the slot centre from the waveguide centre
<b>E</b>	electric field intensity
$\mathbf{E}_0$	electric intensity before introducing losses
$f$	frequency
$f_c$	waveguide cut-off frequency
$f_{cm}$	m-th mode cut-off frequency
$f_{\max}$	maximum oscillation frequency of the transistor
$f_n$	normalization frequency
$f_{\text{stat}}$	limit frequency of using results of quasistatic methods
$f_T$	transit time cut-off frequency of a transistor
$F_{\min}$	minimum noise figure
$g, g_m$	normalized slot width, transconductans for $U_S = 0$ V, respectively
$g_i$	values of prototype elements

$G$	conductivity
$G_a$	available power gain
$G(x, y; x', y')$	Green's function
$h$	substrate thickness
$h_1$	height of the dielectric layer under substrate
$h_2$	height of dielectric layer above substrate
$h_{21e}$	current gain of the transistor in common emitter configuration
$H$	magnetic field intensity
$H_0$	magnetic field intensity before introducing losses
$I$	longitudinal current in the strips; isolation attenuation
$I_{dss}$	drain current of transistor
$I_L$	transition attenuation (loss)
$J$	surface current density
$J_{xin}(\beta)$	Fourier image of the base function of the current density
$k$	wave number
$k_c$	equivalent dielectric constant at the limit frequency
$k_e$	equivalent dielectric constant
$k, k_i, k', k'_i$	moduli of elliptic integral
$K(k), K(k_i)$	complete elliptic integral of first type
$K'(k), K'(k_i)$	complementary elliptic integral of first type
$l_i$	length of the line segment
$l_o$	length of the capacity of the stub
$l_r$	resonator length
$l_s$	active segment length
$L$	inductance; coupling attenuation of a coupler
$n$	number of vertices of $n$ -angle; filtre degree
$n_j$	normal line to the $j$ -th part of the conductor
$N$	number of conductive strips
$N_n(kr)$	Bessel's function of second type of $n$ -th order

---

$p$	approximation coefficient; complex frequency; auxiliary constant
$P, P_{\max}$	power, maximum power
$p$	dipole moment
$P(f)$	correcting function
$q$	approximation coefficient, filling factor, number of transfer zeros
$q_s$	correction for screening
$q_t$	correction for the microstrip thickness
$Q$	charge on the strip
$r$	cylindrical coordinate
$r_i$	internal diameter of a radial stub
$r_L$	external diameter of a radial stub
$R, R_0$	resistance, terminating resistance
$R'_b$	equivalent substrate resistance
$RL$	return losses
$R_s, R_{sj}$	specific high frequency resistance, specific high frequency resistance of the $j$ -th part of the conductor surface
$s$	slot width; curve enclosing the strip conductor
$S$	directivity, surface area
$S_v$	surface area of the conductor cross section
$S_{12}(j)$	transfer function
$t$	time, conductor thickness
$u$	normalized conductor width
$U$	voltage at the strip centre
$U_{DS}$	drain-source voltage
$U_p, U_P$	breakdown voltage, pinch-off voltage, respectively
$v_f$	phase velocity
$v$	wave velocity
$V, V_1, V_2, V_3$	potential of conductors
${}_k V_m^i$	input voltage pulse from direction $m$

$k+1 V_n^r$	reflected voltage pulse in direction $n$
$w$	complex variable; conductor width
$w'$	corrected strip width
$w_c, w_L, w_1, w_2$	conductor width
$w_{ef}$	effective strip width
$W$	wave energy per unit length
$x, x', x_b$	parameter
$x, x_i$	Cartesian coordinate
$x$	charge coordinate
$y, y_i$	Cartesian coordinate
$\mathbf{y}$	unit vector in direction of $y$ -axis
$y'$	charge coordinate
$Y_0$	characteristic admittance
$Y_{0p}$	characteristic admittance of a capacitive sub
$z$	Cartesian coordinate; complex variable
$Z_i$	input wave impedance
$Z_T$	input terminal impedance
$Z_0, Z_{0A}$	characteristic impedance
$Z_{0\infty}$	characteristic impedance for $f \rightarrow \infty$
$Z_0(kr)$	wave impedance of radial line
$Z_{0e}, Z_{0o}$	characteristic impedance of even and odd modes respectively
$\alpha$	attenuation constant, current gain, relaxation constant
$\alpha_0$	current gain at zero frequency
$\alpha_C$	conductive losses of unit length line
$\alpha_d$	attenuation constant of the TEM mode resulting from dielectric losses
$\alpha_D$	dielectric losses of unit length line
$\alpha_i$	vertex angle
$\alpha_r$	centre angle of radial stub
$\alpha_l$	temperature coefficient of the length expansivity

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$\alpha_z$	transformation parameter
$\alpha_{\varepsilon_r}$	temperature coefficient of relative permittivity
$\beta$	phase constant, coefficient of voltage coupling
$\gamma$	propagation constant
$\Gamma$	reflection coefficient
$\Gamma_e, \Gamma_o$	reflection coefficient of even and odd modes, respectively
$\delta, \delta_{ef}$	loss angle, effective loss angle
$\delta_n$	penetration depth
$\delta(x - x')$	$\delta$ -function
$\Delta$	increment
$\varepsilon, \varepsilon(\omega)$	permittivity
$\varepsilon_r$	relative permittivity
$\varepsilon_{ef}$	effective permittivity
$\eta_{add}$	adding efficiency
$\Theta$	cylindrical coordinate
$\Theta_i, \Theta_L$	angle
$\lambda_g, \lambda_L$	wave length in line
$\lambda_c$	cut-off wave length
$\mu, \mu_0$	permeability, permeability of vacuum
$\Pi^e, \Pi^m$	Hertz vector
$\rho$	charge density; triangular polar coordinate
$\tau_b, \tau_c, \tau_e$	time of flight through the base, collector, emitter
$\tau_{ec}$	total transistor delay
$\tau_{rc}$	time constant of the collector
$\varphi_d$	differential phase shift
$\Phi, \Phi_k$	potential, potential on the surface of the $k$ -th conductor
$\Phi_D$	scalar dipole potential
$\psi$	angle
$\omega$	angular frequency
$\omega'$	cut-off angular frequency

## **B) Abbreviations**

BFL	Buffered FET Logic
DCFL	Direct Coupled FET Logic
SDFL	Schottky Diode FET Logic
HEMT	High Electron Mobility Transistor
MODFET	MOdulation Doped FET
TEGFET	Two-dimensional Electron Gas FET
SDHT	Selective Doped Heterostructure Transistor
SISFET	Semiconductor Insulator Semiconductor FET
MESFET	MEtal Semiconductor FET
FET	Field Effect Transistor
MIC	Microwave Integrated Circuit
MMIC	Monolithic Microwave Integrated Circuit
SWR	Standing Wave Ratio
VSWR	Voltage Standing Wave Ratio
TEM	Transverse ElectroMagnetic (wave)

# 1

## Introduction

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In general, the origin of the development of microwave circuits dates back to 1930, when microwave systems were introduced, advantageously implemented by waveguide parts. In attempts to provide the efficient transfer of the microwave power from the supply into the waveguide transmission line, considerable effort was developed in the field of the analysis of microwave circuits. Works by P. H. Smith (Smith, 1969) as a designer of graphic means for solving problems of transmission lines are well known. World War II accelerated the progress of the development of microwave procedures, which have found their application in the radar technique. This was a period of the origination of the hybrid T-element and of the first directional coupler and these parts immediately found their use in practice. The classic methods of solving the circuits led to a change from relationships for the voltage and current and impedance and admittance matrices to terms as transmitted and reflected waves, which resulted to a concept of scattering matrices. This opened possibilities of solving multiport networks. In this period, the waveguide and coaxial technique represented elements of microwave circuits and they complemented each other by their characteristics. The waveguide technique was used for its capability to transmit higher powers at low losses. Resonators based on cavity waveguides achieved high quality coefficients  $Q$ . In contrast to this, the coaxial technique offered a wide frequency range due to the absence of dispersion effects. The 1950s were characterized by an origin of special applications of two-conductor lines, as for example the strip line (Barret and Barnes, 1951). The advantage was taken of the feature that the characteristic impedance of the line can be easily controlled by the width of the middle strip, usually produced by the photo-etching technology

on the copperclad dielectric substrate. This technology also found a wider application in the production of directional couplers and power dividers.

The microstrip is a further type of line occurring after that, however, due to larger loss per unit length resulting from radiation and due to its low dielectric constant ( $\varepsilon = 2.5$ ) of the originally considered substrates, it did not find wide use in the microwave technique at that time. This, however, simultaneously initiated the development for a further period.

In the 1960s, a revival of microstrip lines actually occurred. This was also facilitated by the discovery of the elegant analysis of microstrip structures by Wheeler, 1964, which was based on the conformal representation. The new methods and technologies initiated a rapid development in the use of microstrip lines. The abilities of planar microwave transmission structures, rapid development of microwave semiconductor elements, technique of thin layers and photolithography resulted in a development of a new field of the technology — microwave integrated circuits (MIC). We can tell that these circuits mean an extension of the technology of hybrid integrated circuits into microwave frequencies.

The integrated technology plays an important role in the current microwave technique and it represents a key factor in the successful development of the microwave technique and in their penetration into different regions of the science and technology, into electronics for investment as well as consumption purposes. This technology presents a basic assumption of the economically efficient implementation of modern high-frequency systems with excellent technical and operational parameters, high reliability, resistance and stability, which are compact and in comparison with the preceding waveguide systems also characterized by smaller size and weight.

The high-productivity production of microwave integrated circuits and microwave systems on the integrated technological basis with low losses corresponding to the rejection of products and exceeding of allowances desired, is tightly related to a high level of theoretical as well as experimental methods of the microwave integrated circuit design. A wide base of the knowledge, method of the analysis and synthesis and of checked procedures is an ultimate requirement here, since the integrated structure allows at most for minimum repair interventions into the physically accomplished circuits in order that

it could be unnecessary to adjust or alter unsuitable and, due to an imprecise design, deflected values of electric parameters of the integrated circuit. This factor is even more remarkably manifested in the series and mass production of a certain type of the microwave integrated circuit, where the lowest losses considerably affect the economy of the whole production.

The purpose of the authors of the present book is to yield to an expert reader as much information as possible on theoretical methods of analysis and synthesis of microwave elements and circuits produced by the integrated technology. The material arranged in the book is to a considerable extent a result of the research and development works of the authors, and it was also experimentally checked by the authors. The book presents material sufficient for providing its use as a practical handbook for experts in the research, designers of integrated circuits in industry and also as an auxiliary text for students at technical universities. However, the authors are aware that the current rapid development of the microwave integrated technology cannot be completely described in the monograph.

Chapter 2 deals with the analysis of passive circuit elements starting from transmission lines of different types and their MIC applications. The second part considers discontinuities, their characteristics and applications in the MIC. In the third part, the problems of lumped elements are analysed.

Chapter 3 concerns semiconductor circuit elements such as Schottky diodes, varactor diodes, PIN diodes and transistors (bipolar, MESFET, HEMT).

Chapter 4 considers the basic circuits. The first part is aimed at methods of MIC synthesis with the use of the matrix approach. In the second part, basic linear circuits are analysed (non-reflecting load, resonators, attenuators, etc.) and the last part describes basic active and non-linear circuit (detectors, mixers, oscillators and amplifiers).

Chapter 5 includes the problems of measuring and testing. The first part considers measuring methods from the metrological standpoint. In the second part, the problems of the measuring set (test fixture and probes) are analysed and in the third part, calibration approaches are discussed. The last part considers the noise measurements.

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## 2

# Analysis of passive circuit elements

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F. Hrníčko and M. Pavel

### 2.1 TRANSMISSION LINES FOR MICROWAVE INTEGRATED CIRCUITS

In the microwave integrated circuits (MICs) special types of lines are used that, in general, are formed by means of diverse configurations of conducting strips on different substrates. The latter are represented by various types of lines such as microstrip, coplanar, slotlines or transmission lines on suspended or multi-layer substrates as well as coupled lines. For some important types of lines accurate solutions for quasi-static approximations were obtained, whereby the line's dispersion was determined with the use of a series of numerical methods that for the purpose of computer aided design can be approximated by closed relationships and vice versa the relationships for the synthesis can also be obtained.

#### 2.1.1 Basic characteristics of homogeneous transmission lines

Basic component of the MIC is formed by homogeneous transmission lines enabling transmission of the electromagnetic field energy from the generator to the load or they stand as a part of a distributed circuit design. Usually, strip conductors located in definite places at dielectric sheets interfaces are used. Further, we shall confine ourselves just to the structures showing longitudinal uniformity. Transverse dimensions of such a line are independent of the coordinate along the direction of propagation. Basic parameters of the line are found using CAD-approximations or more tedious analytical methods from its dimensions in the transverse plane.

In the transmission lines used in the MICs, various types of waves can be excited. Apart from the waves propagating along the interface formed by the dielectric substrates waves can also be induced that are radiated into surrounding space. We try to suppress such unwanted waves by a suitable choice of transverse line dimensions and in the way the circuit is fed.

Transmission lines structure can be classified as *open*, *side-open* or *closed*. This classification says in what type of space the electromagnetic energy is propagating. By computation, various numerical solutions of the field are obtained differing both by their character and formal description. Open MIC lines are not resistant against perturbations and they, themselves can become a source of disturbance if the transverse dimensions of the structure are chosen improperly. On the other side, the improper transmission of information on the lines in closed structures is not affected by external fields. Most popular transmission lines in open structures are microstrip, coplanar waveguide, coplanar strips, slotline, suspended microstrip line, and some other lines. These types of lines, as a rule are enclosed in conductive boxes whose effect can either be neglected under the assumption of the properly selected size. In the other case the closed transmission structure should be investigated. To the closed structures the lines belong such as stripline, suspended stripline, finline etc. In many cases the closed structure transmission line problem can be analysed as a side-open one advantageously.

Transverse arrangement of some transmission lines for MICs are depicted in Fig. 2.1. In the following chapters the brief description of their properties, the way and limits of their application and accurate closed-form equations are given. They are most often achieved by many parameter curve fitting of precise analytical results. Some of the analytical methods are presented in Chapter 2.1.8 (or in the Appendix). More precise elaborating of those methods lies beyond the scope of this book.

Practically speaking, what we are interested in is the propagation along the transmission lines mentioned in the above. It is necessary to determine the distribution of the intensity of both the electric and magnetic field for the propagation mode under study. It can be achieved by solving the wave equations under definite boundary conditions.

Multiconductor transmission lines enable purely TEM or non-